Directions:

- 1. Section: Math251
- 2. Write your name with one character in each box below.
- 3. Show all work. No credit for answers without work.
- 4. This assessment is closed book and closed notes. You may not use electronic devices, including calculators, laptops, and cell phones.

Academic Integrity Statement: I will complete this work on my own without assistance, knowing or otherwise, from anyone or anything other than the instructor. I will not use any electronic equipment or notes (except as permitted by an existing official, WVU-authorized accommodation).

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- 1. [2 parts, 6 points each] A particle travels in a straight line at constant speed. At time t = 0, the particle is at P(2, -1, 4), and at time t = 1, the particle is at Q(5, 0, 3).
 - (a) Find parametric equations for the position of the particle at time t.

- (b) Find the speed of the particle.
- 2. [6 points] A particle starts at P(1,2,3) at time t=0 and has velocity vector $\mathbf{r}'(t) = \langle 2t, \sin t, t^2 \rangle$. Find the position vector $\mathbf{r}(t)$.

3. [8 points] A particle has position vector $\mathbf{r}(t) = \langle t^2, t, t^2 - 3t \rangle$. Find the minimum speed of the particle.

- 4. [3 parts, 8 points each] Let $\mathbf{r}(t) = \langle t, t^2, t^3 \rangle$ and note that at t = 1, the normal vector \mathbf{N} equals $\frac{1}{\sqrt{2 \cdot 7 \cdot 19}} \langle -11, -8, 9 \rangle$.
 - (a) Find the tangent vector \mathbf{T} and binormal vector \mathbf{B} at t=1.

(b) Find vector equations for the normal plane and osculating plane at time t=1.

(c) Find the radius and center of the osculating circle at t=1.

- 5. Let $f(x,y) = x \sin(2x + 3y)$.
 - (a) [12 points] Find all first and second partials of f(x, y).

(b) **[6 points]** Find a vector equation for the tangent plane to the graph of f(x,y) at $(\pi/4, 0, \pi/4)$.

- 6. [2 parts, 6 points each] The temperature at a point (x, y, z) is given by the function $T(x, y, z) = x^2y + 3z^2$.
 - (a) Find the rate of change in temperature if we start at (1, -3, 2) and move toward the origin.

(b) Starting at (1, -3, 2), we want to increase the temperature is quickly as possible. In which direction should we travel, and what is the rate of increase?

7. [10 points] Let $f(x, y, z) = \ln(x^2 + y^2 + z^2)$ and let x(s, t) = 2s + 3t, y(s, t) = st, and $z(s, t) = s^2 e^t$. Compute $\frac{\partial f}{\partial s}$ when s = 2 and t = 0.

8. [10 points] Find and classify the critical points of $f(x,y) = xy^2 - x^2y + 4x - 4y$ as local minima, local maxima, or saddle points.